## The Political Economy of Currency Unions

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Introduction •00000		Gains and Correlation
Introduction		

• How can monetary policy sustain a currency union when member states have an exit option?

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- Can the central bank with interest rate policy alone save the union?

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- Main contribution:
  - Derive an interest rate rule with state-dependent country weights that can prevent a break-up
  - Spell out conditions under which such a rule works and when not
  - Show which countries are expected to bear the burden

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  - Show which countries are expected to bear the burden
- Preview: Central bank has limits, the rule is not fully credible as it only extends lifetime of the union for a while. Fiscal policy is more potent

Introduction 00000		Gains and Correlation
Setup		

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- These two countries are in a currency union

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- Benefits: Trade of goods is easier with common currency Trade
- Costs: The exchange rate as an important shock absorber is missing
  - Lack of exchange rate is especially costly when **asymmetric shock** hits the union
  - That is the situation in which introducing a national currency is attractive (the outside option)

# Exiting the Union

Two-sided limited commitment to the currency union

- Governments decide unilaterally if they leave the currency union
- Utility of the representative household in the member state is decisive.
- Asymmetric shock. Trade benefits of currency union are outweighed by stabilization costs for one country

# What can a Central Bank do?

Big Asymmetric (productivity) shock. What can the bank do?

- Interest rate ↑ (or ↓). Intertemp. subst.: Consumption ↓ (or ↑)
- $\bullet\,$  But: One-size fits all instrument for currency union.  $\to\,$  affects demand everywhere
- One country would like to have higher, the other lower interest rates
- The central bank **trades off costs** of one country **with benefits** of another
- How far can the central bank go?
- How important are trade gains and bus. cycle synchronicity?
- Does one country benefit?
- Spell out conditions under which CB can save the union

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- The union eventually collapses if a sequence of sufficiently large shocks hit
- Fiscal transfers are more potent, Italy-Germany union survives (but not UK-Germany union)
- More open country (Germany) pays net-transfers

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The Political Economy of Currency Unions

Introduction 00000		Gains and Correlation

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- Exit Options in a Union: Fuchs and Lippi (2006), Ferrari et al. (2019), Eijffinger (2018)
- Fiscal and Monetary Policy in a Union: Auclert and Rognlie (2014), Farhi and Werning (2017), limited commitment and debt restructuring: Müller et al. (2019), Abraham et al. (2019)

Model	Gains and Correlation
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### Model Structure

Follow Corsetti and Pesenti (2002): Home (H) and Foreign (F) country

Firms

- Two types of good, H and F, imperfect substitutes
- No capital, each country produces varieties of goods
- Prices set one period in advance. Producer Currency Pricing
- Monopolistic markets, trade costs when exporting

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- Supply labor
- Can borrow/lend in international financial markets

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Model o●oooo	Gains and Correlation

### Government

### National fiscal authorities

- $\bullet$  Subsidies  $\tau$  to eliminate monopolistic markups
- Lump-sum taxes for households, balanced budget

Model o●oooo	Gains and Correlation

# Government

### National fiscal authorities

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- Lump-sum taxes for households, balanced budget

### Central bank(s)

- Sets interest rates
- Monetary policy under commitment
- Currency Union
- National Currency as outside option
- **Producer Currency Pricing (PCP)** and flexible exchange rate give most favorable outside option, other pricing in robustness

	Model		Gains and Correlation
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# Policy with National Currencies

National central bank acts under commitment: Discretion

$$\max_{\{i_t(s^t)\}_{t=0}^{\infty}} \sum_{t=0}^{\infty} \sum_{s^t \in \mathcal{A}} \beta^t p(s^t \mid s^0) \left( \log(C_t(s^t)) - \kappa L_t(s^t) \right)$$

subject to equilibrium conditions

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subject to equilibrium conditions

Optimal national monetary policy under PCP: Price stability  $\rightarrow$  Rigid prices are main friction, optimally firm's marginal costs are stabilized:

$$MC_t = \mathbb{E}_{t-1}[MC_t]$$

 $\rightarrow$  Exchange rate is flexible.

 $\rightarrow$  Flex price allocation with trade costs can be replicated for all states.

# Policy in a Currency Union

Union-wide central bank acts under commitment, weight for H is  $\xi$ 

$$\begin{split} \max_{\{i_t^{EU}\}_{t=k}^{\infty}} & \xi \sum_{t=0}^{\infty} \sum_{s^t \in A} \beta^t p(s^t \mid s^0) \left( \log(C_t(s^t)) - \kappa L_t(s^t) \right) \\ & + (1-\xi) \sum_{t=0}^{\infty} \sum_{s^t \in A} \beta^t p(s^t \mid s^0) \left( \log(C_t^*(s^t)) - \kappa L_t^*(s^t) \right) \end{split}$$

subject to equilibrium conditions and weight  $\xi$  for H

Optimal union-wide policy: Price stability for the union.



# Policy in a Currency Union

 $\rightarrow$  Weighted average of marginal costs is stabilized:

$$1 = \left(\underbrace{\left(\xi\gamma + (1-\xi)(1-\gamma)\right)}_{\text{Effective weight for H}} \frac{MC_t}{\mathbb{E}_{t-1}[MC_t]} + \left(\xi(1-\gamma) + (1-\xi)\gamma\right)\frac{MC_t^*}{\mathbb{E}_{t-1}[MC_t^*]}\right)^{-1}$$

Effective weight depends on country weight  $\xi$  and home bias  $\gamma$ 

# Policy in a Currency Union

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Effective weight depends on country weight  $\xi$  and home bias  $\gamma$ 

- $\xi\uparrow$  and  $\gamma\uparrow$ , more weight on home's marginal costs
- $\rightarrow$  Fixed exchange rate, no trade costs
- $\rightarrow$  Flex price allocation can only be replicated, if productivity the same

Model	Gains and Correlation
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## Calibration, SMM

- Symmetric country calibration (asymmetric in robustness)
- Consider a range of trade gains from a currency union, here 4.6% and 6.5%
- Calibrate shocks that match correlation of GDP growth and volatility for Gemany-**Italy** union and Germany-**UK** union

	Italy	UK	Description
Parameters			
ρ	0.66	0.73	weight on local shock
σ	3.48	3.68	variance of shock process
Moments			
GDP correlation data	0.75	0.59	GDP correlation 1970-2020
GDP correlation model	0.75	0.59	GDP correlation in the model
GDP volatility data GDP volatility model	2.71 2.71	2.70 2.73	St. dev. of GDP growth 1970-2020 St. dev. of GDP growth in the model

#### Table: SMM Calibration

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### Model Experiment

Run several simulation under four scenarios

In each scenario outside option is the same. Only policy within the union differs.

Experiment	Transfers	Interest rates
1. National Planner	-	-
2. Union-wide Ramsey Planner	$\checkmark$	-
3. Union-wide Central Bank	-	$\checkmark$
4. Transfers & Mon Pol	$\checkmark$	$\checkmark$

 $\Rightarrow$  Exit options add occasionally binding participation constraints

		Simulation	Gains and Correlation
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## Optimal Monetary Policy with Exit Option

Old monetary stance if countries cannot exit

$$1 = \left( \left( \frac{\xi \gamma + (1 - \xi)(1 - \gamma)}{\mathbb{E}_{t-1}[MC_t]} + \left( \frac{\xi}{(1 - \gamma)} + (1 - \xi)\gamma \right) \frac{MC_t}{\mathbb{E}_{t-1}[MC_t^*]} \right)^{-1}$$

**New** monetary stance with exit option

$$1 = \left(\frac{1 - \gamma + \lambda(s^t)\gamma}{1 + \lambda(s^t)} \frac{MC_t}{\mathbb{E}_{t-1}[MC_t]} + \frac{\gamma + \lambda(s^t)(1 - \gamma)}{1 + \lambda(s^t)} \frac{MC_t^*}{\mathbb{E}_{t-1}[MC_t^*]}\right)^{-1}$$

 $\Rightarrow \lambda(s^t)$  state-dependent country weight for H

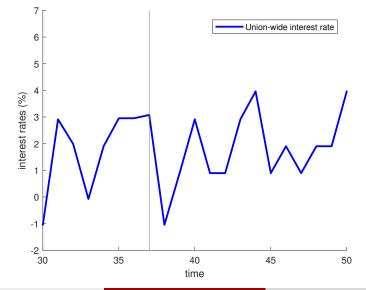
	Simulation 0000000	Gains and Correlation
Intuition		

Once a shock comes that makes H willing to leave

- Central bank adjusts interest rates and affects economic activity today
- It announces to do more favorable policy for the crisis country in the future
- Relative weight  $\lambda(s^t)$  persistently increases, until another big shock hits the union

	Simulation	Gains and Correlation
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## Simulation Interest Rate Path: No Exit Option

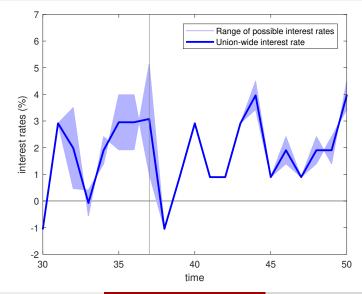


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The Political Economy of Currency Unions

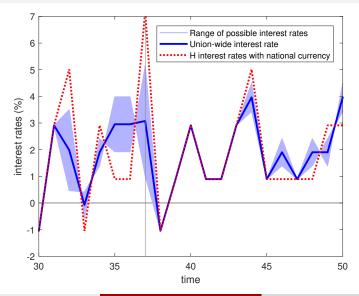
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## Simulation Interest Rate Path: Set of Possible Rates



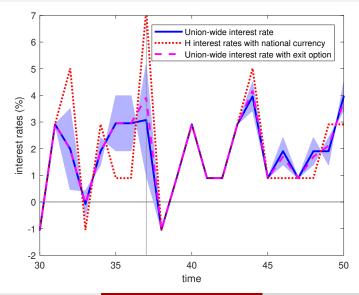
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## Simulation Interest Rate Path: With National Currency



	Simulation	Gains and Correlation
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## Simulation Interest Rate Path: With Exit Option



# Break-up with High Trade Gains

#### Table: Break-up under different planners, trade gains 6.5%

Planner Allocation		break-up next eriod		uration of the union	Avera	ge Gain
	UK	lta	UK	lta	UK	lta
National	2.15%	0%	67	100001	0.016654	0.018692
Fiscal	0%	0%	100001	100001	0.016661	0.018692
Monetary	0%	0%	100001	100001	0.016939	0.018692
Fiscal & Monetary	0%	0%	100001	100001	0.01686	0.018692
First best	0%	0%	100001	100001	0.020814	0.020814

	Gains and Correlation •000000

### Lower Trade Gains

Consider a large simulation with lower trade gains of 4.6%:

- Gains of union turn negative more frequently, countries would exit more frequently Gains
- Larger amount of transfers needed (0.1% of GDP per period). Union can still be sustained with transfers Transfers
- Monetary policy cannot sustain the union, only able to extend the lifetime of an unstable currency union a bit

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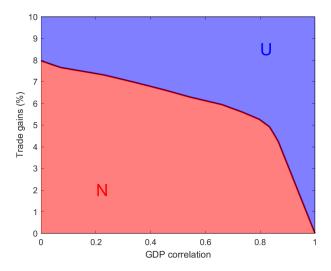
## Results with low trade gains

#### Table: Break-up under different planners, trade gains 4.6%

Planner Allocation		break-up next eriod		uration of the union	Avera	ge Gain
	UK	lta	UK	lta	UK	lta
National	46.30%	2.29%	3	62	0.0047635	0.010301
Fiscal	0%	0%	100001	100001	0.0090647	0.010555
Monetary	2.15%	2.29%	67	62	0.0086743	0.0098041
Fiscal & Monetary	0%	0%	100001	100001	0.0092006	0.010467
First best	0%	0%	100001	100001	0.012665	0.012665

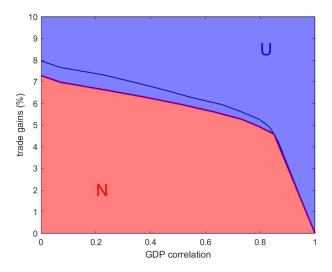
	Gains and Correlation

## Sustainability Frontier: National Planner



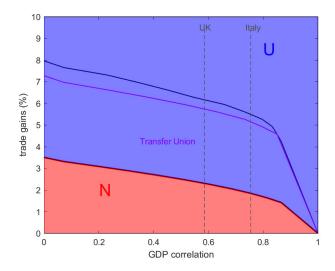
	Gains and Correlation

# Sustainability Frontier: Monetary Policy



	Gains and Correlation 0000●00

## Sustainability Frontier: Transfers

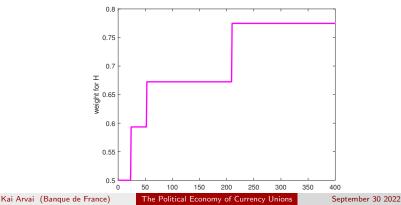


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#### Robustness, asymmetric countries

- Change PCP assumption to LCP or intermediate values
- Consider asymmetric countries
- If F is more open, it benefits more from trade in union

F never hits participation constraint, H's weight for CB with exit option converges to fix values



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Introduction	Model	Simulation	Gains and Correlation
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Conclusion			

- Monetary policy alone cannot sustain currency union
- Central bank can only extend the lifetime of an unstable currency union for some time
- It requires other interventions than monetary policy to prevent exit by a member state
- Larger gains and higher GDP growth correlation increase stability. A union with the UK seems less stable.

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## Trade Benefits

- The paper models the costs of a currency union in detail, not the gains
- The gains in form of more trade of goods in the steady state is by assumption
- Think about the elimination of currency conversion costs and more complicated contracts with different currencies
- Trade gains can also be thought as break-up costs: If currency union breaks up, you have to make a new trade deal
- Baier et al. (2014). Customs Unions & common market increase bilateral trade by a lot! Country that exits the union might have to exit these agreements as well.



## Households

• Countries H and F with representative households.

$$\mathbb{E}\bigg[\sum_{\tau=t}^{\infty}\beta^{\tau-t}\bigg(\ln(C_{\tau})-\kappa L_{\tau}\bigg)\bigg]$$

•  $C_t$  is basket of home and foreign goods with home bias  $\gamma$ 

$$C_t = C_{H,t}^{\gamma} C_{F,t}^{1-\gamma}, \quad C_t^* = C_{H,t}^{*1-\gamma} C_{F,t}^{*\gamma}$$
  
• Varieties h:  $C_{H,t} = \left[\int_0^1 C(h)^{\frac{\theta-1}{\theta}} dh\right]^{\frac{\theta}{\theta-1}}$ 

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- Varieties h:  $C_{H,t} = \left[\int_0^1 C(h)^{\frac{\theta-1}{\theta}} dh\right]^{\frac{\theta}{\theta-1}}$
- The budget constraint is given by

$$B_{H,t} + \mathcal{E}_t B_{F,t} + P_{H,t} C_{H,t} + P_{F,t} C_{F,t} + T_t = (1+i_t) B_{H,t-1} + (1+i_t^*) \mathcal{E}_t B_{F,t-1} + W_t L_t + \Pi_{H,t}$$

• Exchange rate  $\mathcal{E}_t$  defined as one unit of home currency per unit of foreign currency,  $i_t$  set by central bank and known in t - 1.

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### Firms

• Input labor  $L_t(h)$  to produce variety h:

```
Y_t(h) = a_t L_t(h)
```

• Stochastic productivity  $a_t$  and  $a_t^*$ 

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$$Y_t(h) = a_t L_t(h)$$

- Stochastic productivity  $a_t$  and  $a_t^*$
- Demand for good h:

$$\left(\frac{p_t(h)}{P_{H,t}}\right)^{-\theta} C_{H,t} + (1+\varpi) \left(\frac{p_t^*(h)}{P_{H,t}^*}\right)^{-\theta} C_{H,t}^*$$

- Iceberg trade costs. If 1 unit is shipped only  $\frac{1}{1+\omega}$  arrives. Trade
- Marginal costs  $MC_t$  and wages  $W_t$ :

$$MC_t(h) = MC_t = a_t^{-1}W_t$$

### Firms: Profits and Pricing

#### • Pricing one period before

- Monopolistic pricing for H's goods in H and F
- Firms maximize their profits

$$\Pi_{t}(h) = \underbrace{\left((1-\tau)p_{t}(h) - MC_{t}\right)\left(\frac{p_{t}(h)}{P_{H,t}}\right)^{-\theta}C_{H,t}}_{+ \underbrace{\left((1-\tau)\mathcal{E}_{t}p_{t}^{*}(h) - (1+\varpi)MC_{t}\right)\left(\frac{p_{t}(h)^{*}}{P_{H,t}^{*}}\right)^{-\theta}C_{H,t}^{*}}_{\text{Profits in F}}$$

## **Optimal Prices**

$$p_t(h) = P_{H,t} = \frac{1}{1-\tau} \frac{\theta}{\theta-1} \mathbb{E}_{t-1}[MC_t]$$
$$p_t^*(h) = P_{H,t}^* = (1+\varpi) \frac{1}{1-\tau} \frac{\theta}{\theta-1} \frac{\mathbb{E}_{t-1}[MC_t]}{\mathcal{E}_t}$$

main

## Discretion

$$\max_{\{i_t(s^t)\}_{t=k}^{\infty}} \sum_{t=0}^{\infty} \sum_{s^t \in A} \beta^t p(s^t \mid s^t) \left( \log(C_t(s^t)) - \kappa L_t(s^t) \right)$$

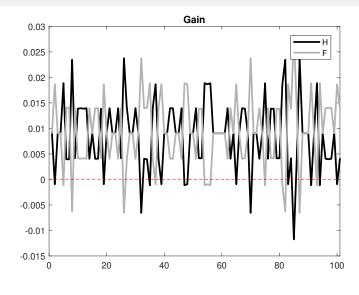
Monetary policy implies that marginal costs follow:

$$P_{Ht} = \Theta \mathbb{E}_{t-1}[MC_t]$$

where  $\Theta$  is the inflationary bias, a function of trade openness, markups and subsidies. The higher the markups and the higher the home bias, the larger the inflationary bias will be, as a central bank tries to inflate away the monopolistic markups.

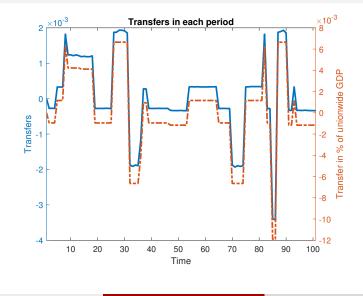
$$\Theta^{*N} = \frac{\gamma}{\frac{1+\gamma\varpi}{\theta^*} \frac{\theta^*}{(\theta^*-1)(1-\tau)(1+\varpi)}} \quad \text{back}$$

## Gains over time with low trade gains



back

## Transfers over time with low trade gains



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Countries H and F with representative households.

$$\mathbb{E}\bigg[\sum_{\tau=t}^{\infty}\beta^{\tau-t}\bigg(\ln(C_{\tau})-\kappa L_{\tau}\bigg)\bigg]$$

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Exchange rate  $\mathcal{E}_t$  defined as one unit of home currency per unit of foreign currency.

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### Firms

Input labor  $L_t(h)$  to produce variety h:

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Stochastic productivity  $a_t$  and  $a_t^*$ .

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Stochastic productivity  $a_t$  and  $a_t^*$ . Demand for good h is:

$$\left(\frac{p_t(h)}{P_{H,t}}\right)^{-\theta}C_{H,t}+(1+\varpi)\left(\frac{p_t^*(h)}{P_{H,t}^*}\right)^{-\theta}C_{H,t}^*.$$

Iceberg trade costs. If 1 unit is shipped only  $\frac{1}{1+\omega}$  arrives.

Marginal costs  $MC_t$  and wages  $W_t$ .

$$MC_t(h) = MC_t = a_t^{-1}W_t$$

# Firms: Profits and Pricing

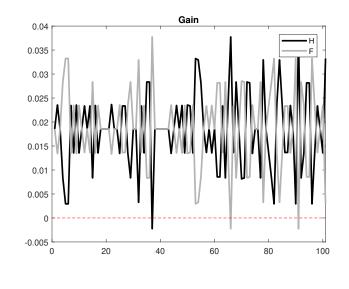
Profits are :

$$\Pi_{t}(h) = \underbrace{\left((1-\tau)p_{t}(h) - MC_{t}\right) \left(\frac{p_{t}(h)}{P_{H,t}}\right)^{-\theta} C_{H,t}}_{+ \underbrace{\left((1-\tau)\mathcal{E}_{t}p_{t}^{*}(h) - (1+\varpi)MC_{t}\right) \left(\frac{p_{t}(h)^{*}}{P_{H,t}^{*}}\right)^{-\theta} C_{H,t}^{*}}_{\text{Profits in F}}$$

Pricing one period before: Monopolistic pricing for H's goods in H and F

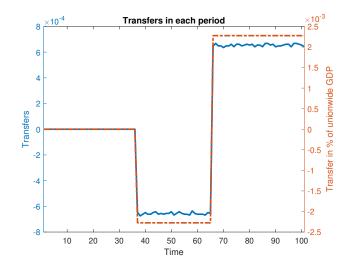
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# Break-up: Simulating Gain over time



Transfers

## 2. Ramsey Planner: Optimal Transfer in each Period



Gains

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# Mechanism and Intuition for Monetary Policy

Why are currency unions costly? Example of an asymmetric shock.

• **Productivity**  $\downarrow$  in Home country.  $\rightarrow$  **Marginal costs**  $\uparrow$ 

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- Households in Home need to work too much, utility goes down
- With a national currency & focus on price stability: Interest rates ↑, exchange rate appreciates and prices ↑ of home goods for foreigners
- In a currency union this adjustment does not happen